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## Description

cvpermute() returns all permutations of the values of column vector $V$, one at a time. If $V=(1 \backslash 2 \backslash 3)$, there are six permutations and they are $(1 \backslash 2 \backslash 3),(1 \backslash 3 \backslash 2),(2 \backslash 1 \backslash 3),(2 \backslash 3 \backslash 1),(3 \backslash 1 \backslash 2)$, and $(3 \backslash 2 \backslash 1)$. If $V=(1 \backslash 2 \backslash 1)$, there are three permutations and they are $(1 \backslash 1 \backslash 2)$, $(1 \backslash 2 \backslash 1)$, and $(2 \backslash 1 \backslash 1)$.

Vector $V$ is specified by calling cvpermutesetup(),

```
    info = cvpermutesetup(V)
```

info holds information that is needed by cvpermute() and it is info, not $V$, that is passed to cvpermute(). To obtain the permutations, repeated calls are made to cvpermute() until it returns J ( $0,1,$. ):

```
info = cvpermutesetup(V)
while ((p=cvpermute(info)) != J(0,1,.)) {
        ... p ...
    }
```

Column vector $p$ will contain a permutation of $V$.
cvpermutesetup() may be specified with one or two arguments:

```
info = cvpermutesetup (V)
info = cvpermutesetup ( }V\mathrm{ , unique)
```

unique is usually not specified. If unique is specified, it should be 0 or 1 . Not specifying unique is equivalent to specifying unique $=0$. Specifying unique $=1$ states that the elements of $V$ are unique or, at least, are to be treated that way.

When the arguments of $V$ are unique-for instance, $V=(1 \backslash 2 \backslash 3)$ —specifying unique $=1$ will make cvpermute() run faster. The same permutations will be returned, although usually in a different order.

When the arguments of $V$ are not unique-for instance, $V=(1 \backslash 2 \backslash 1)$-specifying unique $=1$ will make cvpermute () treat them as if they were unique. With unique $=0$, there are three permutations of $(1 \backslash 2 \backslash 1)$. With unique $=1$, there are six permutations, just as there are with $(1 \backslash 2 \backslash 3)$.

## Syntax

$$
\text { info }=\text { cvpermutesetup }(\text { real colvector } V[, \text { real scalar unique }])
$$

real colvector cvpermute (info)
where info should be declared transmorphic.

## Remarks and examples

## Example 1

You have the following data:

| v1 | v2 |
| :--- | :--- |
| 22 | 29 |
| 17 | 33 |
| 21 | 26 |
| 20 | 32 |
| 16 | 35 |

You wish to do an exact permutation test for the correlation between v 1 and v 2 .
That is, you wish to (1) calculate the correlation between v1 and v2-call that value r-and then (2) calculate the correlation between v 1 and v 2 for all permutations of v 1 , and count how many times the result is more extreme than $r$.

For the first step,

```
X = (22, 29 \
> 17, 33\
> 21, 26 \
> 20,32\
> 16, 35)
: correlation(X)
[symmetric]
```

1
2
symmetric] 1


The correlation is -0.846855 . For the second step,

```
V1 = X[,1]
V2 = X[,2]
num = den = 0
info = cvpermutesetup(V1)
while ((V1=cvpermute(info)) != J(0,1,.)) {
    rho = correlation((V1,V2))[2,1]
    if (rho<=-.846 | rho>=.846) num++
    den++
}
```

```
: (num, den, num/den)
```

    1 2 3
    1

| 13 | 120 | .1083333333 |
| :--- | :--- | :--- |

Of the 120 permutations, $13(10.8 \%)$ were outside 0.846855 or -0.846855 .

## > Example 2

You now wish to do the same thing but using the Spearman rank-correlation coefficient. Mata has no function that will calculate that, but Stata has a command that does-see $[R]$ spearman-so we will use the Stata command as our subroutine.

This time, we will assume that the data have been loaded into a Stata dataset:

```
list
```

For the first step,

```
. spearman var1 var2
Number of observations = 5
    Spearman's rho = -0.9000
Test of HO: var1 and var2 are independent
                        Prob = 0.0468
```

For the second step,

```
V1 = st_data(., "var1")
info = cvpermutesetup(V1)
num = den = 0
while ((V1=cvpermute(info)) != J(0,1,.)) {
    st_store(., "var1", V1)
    stata("quietly spearman var1 var2")
    rho = st_numscalar("r(rho)")
    if (rho<=-.9 | rho>=.9) num++
    den++
}
(num, den, num/den)
                            1 2 3
1
\begin{tabular}{|lll|}
\hline 2 & 120 & .0166666667 \\
\hline
\end{tabular}
```

Only two of the permutations resulted in a rank correlation of at least 0.9 in magnitude.

In the code above, we obtained the rank correlation from $r$ ( $r h o$ ) which, we learned from $[R]$ spearman, is where spearman stores it.

Also note how we replaced the contents of var1 by using st_store(). Our code leaves the dataset changed and so could be improved.

## Conformability

cvpermutesetup ( $V$, unique):

| $V:$ | $n \times 1$ |  |
| ---: | :--- | :--- |
| unique: | $1 \times 1$ | (optional) |
| result: | $1 \times L$ |  |

cvpermute (info):

$$
\begin{aligned}
\text { info: } & 1 \times L \\
\text { result: } & n \times 1 \text { or } 0 \times 1
\end{aligned}
$$

where

$$
L= \begin{cases}3 & \text { if } n=0 \\ 4 & \text { if } n=1 \\ (n+3)(n+2) / 2-6 & \text { otherwise }\end{cases}
$$

The value of $L$ is not important except that the info vector returned by cvpermutesetup() and then passed to cvpermute() consumes memory. For instance,

| $n$ | $L$ | Total memory $(8 \times L)$ |
| ---: | ---: | :---: |
| 5 | 22 | 176 bytes |
| 10 | 72 | 576 |
| 50 | 1,372 | 10,560 |
| 100 | 5,247 | 41,976 |
| 1,000 | 502,497 | $4,019,976$ |

## Diagnostics

cvpermute() returns $J(0,1,$.$) when there are no more permutations.$

## Also see

[M-4] Statistical - Statistical functions
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