# Title

cmrologit - Rank-ordered logit choice model

Description Options Acknowledgment Quick start Remarks and examples References Menu Stored results Also see Syntax Methods and formulas

# Description

cmrologit fits the rank-ordered logistic regression model by maximum likelihood (Beggs, Cardell, and Hausman 1981). This model is also known as the Plackett-Luce model (Marden 1995), as the exploded logit model (Punj and Staelin 1978), and as the choice-based method of conjoint analysis (Hair et al. 2010).

# Quick start

Rank-ordered logit model of rankings y on x1, x2, and x3, using cmset data cmrologit y x1 x2 x3

Same as above, but interpret the lowest value of y as the best cmrologit y x1 x2 x3, reverse

Use Efron's method for handling ties in rankings cmrologit y x1 x2 x3, ties(efron)

With cluster-robust standard errors for clustering by levels of cvar cmrologit y x1 x2 x3, vce(cluster cvar)

### Menu

Statistics > Choice models > Rank-ordered logit model

## Syntax

## cmrologit depvar indepvars [if] [in] [weight] [, options]

options	Description
Model	
<u>inc</u> omplete(#)	use # to code unranked alternatives; default is incomplete(0)
<u>rev</u> erse	reverse the preference order
<pre>ties(spec)</pre>	method to handle ties: exactm, breslow, efron, or none
altwise	use alternativewise deletion instead of casewise deletion
<u>note</u> strhs	keep right-hand-side variables that do not vary within case
<pre>offset(varname)</pre>	include varname in model with coefficient constrained to 1
SE/Robust	
vce( <i>vcetype</i> )	<i>vcetype</i> may be oim, <u>r</u> obust, <u>cl</u> uster <i>clustvar</i> , <u>boot</u> strap, or <u>jack</u> knife
Reporting	
<u>l</u> evel(#)	set confidence level; default is level(95)
display_options	control columns and column formats, row spacing, line width, display of omitted variables and base and empty cells, and factor-variable labeling
Maximization	
maximize_options	control the maximization process; seldom used
<u>coefl</u> egend	display legend instead of statistics
You must cmset your o	data before using cmrologit; see [CM] cmset.
indepvars may contain	factor variables; see [U] 11.4.3 Factor variables.
bootstrap, by, colle	ct, fp, jackknife, and statsby are allowed; see [U] 11.1.10 Prefix commands.
Weights are not allowed	l with the bootstrap prefix; see [R] bootstrap.
fweights, iweights, a are not allowed with	nd pweights are allowed, except no weights are allowed with ties(efron), and pweights a ties(exactm); see [U] 11.1.6 weight.

coeflegend does not appear in the dialog box.

See [U] 20 Estimation and postestimation commands for more capabilities of estimation commands.

# Options

Model

- incomplete(#) specifies the numeric value used to code alternatives that are not ranked. It is assumed that unranked alternatives are less preferred than the ranked alternatives (that is, the data record the ranking of the most preferred alternatives). It is not assumed that subjects are indifferent between the unranked alternatives. The default is incomplete(0).
- reverse specifies that in the preference order, a higher number means a less attractive alternative. The default is that higher values indicate more attractive alternatives. The rank-ordered logit model is not symmetric in the sense that reversing the ordering simply leads to a change in the signs of the coefficients.

ties(*spec*) specifies the method for handling ties (indifference between alternatives) (see [ST] **stcox** for details):

<u>ex</u> actm	exact marginal likelihood (default)
<u>bre</u> slow	Breslow's method (default if pweights specified)
<u>efr</u> on	Efron's method (default if robust VCE)
none	no ties allowed

- altwise specifies that alternativewise deletion be used when omitting observations because of missing values in your variables. The default is to use casewise deletion; that is, the entire group of observations making up a case is omitted if any missing values are encountered. This option does not apply to observations that are excluded by the if or in qualifier or the by prefix; these observations are always handled alternativewise regardless of whether altwise is specified.
- notestrhs suppresses the test that the independent variables vary within (at least some of) the cases. Effects of variables that are always constant are not identified. For instance, a rater's gender cannot directly affect his or her rankings; it could affect the rankings only via an interaction with a variable that does vary over alternatives.

offset(varname); see [R] Estimation options.

SE/Robust

vce(vcetype) specifies the type of standard error reported, which includes types that are derived from asymptotic theory (oim), that are robust to some kinds of misspecification (robust), that allow for intragroup correlation (cluster *clustvar*), and that use bootstrap or jackknife methods (bootstrap, jackknife); see [R] vce\_option.

If ties(exactm) is specified, *vcetype* may be only oim, bootstrap, or jackknife.

Reporting

level(#); see [R] Estimation options.

```
display_options: noci, nopvalues, noomitted, vsquish, noemptycells, baselevels,
allbaselevels, nofvlabel, fvwrap(#), fvwrapon(style), cformat(% fmt), pformat(% fmt),
sformat(% fmt), and nolstretch; see [R] Estimation options.
```

Maximization

```
maximize_options: iterate(#), trace, [no]log, tolerance(#), ltolerance(#),
nrtolerance(#), and nonrtolerance; see [R] Maximize. These options are seldom used.
```

The following option is available with cmrologit but is not shown in the dialog box:

coeflegend; see [R] Estimation options.

### **Remarks and examples**

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Remarks are presented under the following headings:

Overview Examples Comparing respondents Incomplete rankings and ties Clustered choice data Comparison of cmrologit and clogit On reversals of rankings

#### Overview

The rank-ordered logit model can be applied to analyze how decision makers combine attributes of alternatives into overall evaluations of the attractiveness of these alternatives. The model generalizes a version of McFadden's choice model, one where alternatives are not explicitly identified. It uses information about the comparison of alternatives, namely, how decision makers rank the alternatives rather than just specifying the alternative that they like best.

cmrologit expects the data to be in long form, similar to clogit (see [R] clogit), in which each of the ranked alternatives forms an observation. The distinction from a McFadden's choice model fit with clogit is that *depvar* in cmrologit records the rankings of the alternatives, whereas for clogit, *depvar* indicates a single chosen alternative by a value not equal to zero. If your data record only one preferred alternative for each case, cmrologit fits the same model as clogit.

cmrologit interprets equal values of *depvar* as ties. The ranking information may be incomplete "at the bottom" (least preferred alternatives). That is, unranked alternatives may be coded as 0 or as a common value that may be specified with the incomplete() option.

All observations related to an individual are linked together by the case ID variable that you specify in cmset. Alternatives are not explicitly identified by an indicator variable, so cmset is used with the noalternatives option. For example, if id is your case ID variable, to cmset your data before running cmrologit, you type

. cmset id, noalternatives

For details on cmset, see [CM] cmset.

#### Examples

A popular way to study employer preferences for characteristics of employees is the quasiexperimental "vignette method". As an example, we consider the research by de Wolf (2000) on the labor market position of social science graduates. This study addresses how the educational portfolio (for example, general skills versus specific knowledge) affects short-term and long-term labor-market opportunities.

De Wolf asked 22 human resource managers (the respondents) to rank order the 6 most suitable candidates of 20 fictitious applicants and to rank order these 6 candidates for 3 jobs, namely, 1) researcher, 2) management trainee, and 3) policy adviser. Applicants were described by 10 attributes, including their age, gender, details of their portfolio, and work experience. In this example, we analyze a subset of the data.

To simplify the output, we dropped, at random, 10 nonselected applicants per case. The resulting dataset includes 29 cases, consisting of 10 applicants each. The data are in long form: observations correspond to alternatives (the applications), and alternatives that figured in one decision task are identified by the variable caseid. We list the observations for caseid==7, in which the respondent considered applicants for a social-science research position.

ist pre	ef female	age gi	rades edui	fit worker	kp boardexp if	caseid==7
pref	female	age	grades	edufit	workexp	boardexp
0	yes	28	A/B	no	none	no
0	no	25	C/D	yes	one year	no
0	no	25	C/D	yes	none	yes
0	yes	25	C/D	no	internship	yes
1	no	25	C/D	yes	one year	yes
2	no	25	A/B	yes	none	no
3	yes	25	A/B	yes	one year	no
4	yes	25	A/B	yes	none	yes
5	no	25	A/B	yes	internship	no
6	yes	28	A/B	yes	one year	yes

(Vignet study employer prefs (Inge de Wolf 2000)) noobs

. use https://www.stata-press.com/data/r18/evignet

Here 6 applicants were selected. The rankings are stored in the variable pref, where a value of 6 corresponds to "best among the candidates", a value of 5 corresponds to "second-best among the candidates", etc. The applicants with a ranking of 0 were not among the best 6 candidates for the job. The respondent was not asked to express his or her preferences among these four applicants, but by the elicitation procedure, it is known that he or she ranks these four applicants below the 6 selected applicants.

The best candidate was a female, 28 years old, with education fitting the job, with good grades (A/B), with 1 year of work experience, and with experience being a board member of a fraternity, a sports club, etc. The profiles of the other candidates read similarly. Here the respondent completed the task; that is, he or she selected and rank ordered the 6 most suitable applicants. Sometimes the respondent performed only part of the task.

pref	female	age	grades	edufit	workexp	boardexp
0	no	25	C/D	yes	none	yes
0	no	25 28	C/D C/D	no	internship	yes yes
0	yes	25	A/B	no	one year	no
2	yes	25	A/B	no	none	yes
2	no	25	A/B	no	none	yes
2	no	25	A/B	no	one year	yes
5	no	25	A/B	no	none	yes
5	no	25	A/B	no	none	yes
5	yes	25	A/B	no	none	no

list	pref	female	age	grades	edufit	workexp	boardexp	if	caseid==18,	noobs
				(1)						

The respondent selected the six best candidates and segmented these six candidates into two groups: one group with the three best candidates and a second group of three candidates that were "still acceptable". The numbers 2 and 5, indicating these two groups, are arbitrary apart from the implied ranking of the groups. The ties between the candidates in a group indicate that the respondent was not able to rank the candidates within the group.

The purpose of the vignette experiment was to explore and test hypotheses about which of the employees' attributes are valued by employers, how these attributes are weighted depending on the type of job (described by variable job in these data), etc. In the psychometric tradition of Thurstone (1927), "value" is assumed to be linear in the attributes, with the coefficients expressing the direction and weight of the attributes. In addition, it is assumed that "valuation" is to some extent a random procedure, captured by an additive random term. For instance, if value depends only on an applicant's age and gender, we would have

```
value(female<sub>i</sub>, age<sub>i</sub>) = \beta_1female<sub>i</sub> + \beta_2age<sub>i</sub> + \epsilon_i
```

where the random residual,  $\epsilon_i$ , captures all omitted attributes. Thus,  $\beta_1 > 0$  means that the employer assigns higher value to a woman than to a man.

Given this conceptualization of value, it is straightforward to model the decision (selection) among alternatives or the ranking of alternatives: the alternative with the highest value is selected (chosen), or the alternatives are ranked according to their value. To complete the specification of a model of choice and of ranking, we assume that the random residual  $\epsilon_i$  follows an "extreme value distribution of type I", introduced in this context by Luce (1959). This specific assumption is made mostly for computational convenience.

This model is known by many names. Among others, it is known as the rank-ordered logit model in economics (Beggs, Cardell, and Hausman 1981), as the exploded logit model in marketing research (Punj and Staelin 1978), as the choice-based conjoint analysis model (Hair et al. 2010), and as the Plackett–Luce model (Marden 1995).

The model coefficients are estimated using the method of maximum likelihood. The implementation in cmrologit uses an analogy between the rank-ordered logit model and the Cox regression model observed by Allison and Christakis (1994); see *Methods and formulas*. The cmrologit command implements this method for rankings, whereas clogit deals with the variant of choices; that is, only the most highly valued alternative is recorded. In the latter case, the model is also known as the Luce–McFadden choice model. In fact, when the data record the most preferred (unique) alternative and no additional ranking information about preferences is available, cmrologit and clogit return the same information, though formatted somewhat differently.

Before we can fit our model, we must cmset our data. The argument to cmset is the case ID variable, which must be numeric. For these data, it is the variable caseid, which identifies respondents. Unlike other choice models, alternatives are not specified; that is, there is no variable identifying specific alternatives across respondents. Alternatives simply have characteristics in this model.

. cmset caseid, noalternatives Case ID variable: caseid Alternatives variable: <none>

. cmrologit p	ref i.female a	ge i.grades	i.edufit	i.worke	xp i.boardexp	if job==1
Iteration 0:	Log likelihoo	d = -95.41	087			
Iteration 1:	Log likelihoo	d = -71.004	807			
Iteration 2:	Log likelihoo	d = -68.045	946			
Iteration 3:	Log likelihoo	d = -67.906	223			
Iteration 4:	Log likelihoo	d = -67.905	657			
Refining estim	nates:					
Iteration 0:	Log likelihoo	d = -67.905	657			
Rank-ordered 1	logit choice m	odel		Number	of obs =	80
Case ID varial	ole: caseid			Number	of cases =	8
Ties adjustmen	nt: No ties in	data		Obs per	case:	
					min =	10
					avg =	10.00
					max =	10
				LR chi2	(7) =	55.01
Log likelihood	d = -67.90566			Prob >	chi2 =	0.0000
	Г					
pref	Coefficient	Std. err.	Z	P> z	[95% conf.	interval]
pref female	Coefficient	Std. err.	Z	P> z	[95% conf.	interval]
pref female yes	Coefficient 4554119	Std. err.	z -1.26	P> z	[95% conf. -1.164052	interval]
pref female yes age	Coefficient 4554119 0851138	Std. err. .3615579 .0822504	z -1.26 -1.03	P> z  0.208 0.301	[95% conf. -1.164052 2463216	interval] .2532285 .0760939
pref female yes age	Coefficient 4554119 0851138	Std. err. .3615579 .0822504	z -1.26 -1.03	P> z  0.208 0.301	[95% conf. -1.164052 2463216	interval] .2532285 .0760939
pref female yes age grades	Coefficient 4554119 0851138	Std. err. .3615579 .0822504	z -1.26 -1.03	P> z  0.208 0.301	[95% conf. -1.164052 2463216	interval] .2532285 .0760939
pref female yes age grades A/B	Coefficient 4554119 0851138 3.144718	Std. err. .3615579 .0822504 .6200539	z -1.26 -1.03 5.07	P> z  0.208 0.301 0.000	[95% conf. -1.164052 2463216 1.929434	interval] .2532285 .0760939 4.360001
pref female yes age grades A/B	Coefficient 4554119 0851138 3.144718	Std. err. .3615579 .0822504 .6200539	z -1.26 -1.03 5.07	P> z  0.208 0.301 0.000	[95% conf. -1.164052 2463216 1.929434	interval] .2532285 .0760939 4.360001
pref female yes age grades A/B edufit	Coefficient 4554119 0851138 3.144718	Std. err. .3615579 .0822504 .6200539	z -1.26 -1.03 5.07	P> z  0.208 0.301 0.000	[95% conf. -1.164052 2463216 1.929434	interval] .2532285 .0760939 4.360001
pref female yes age grades A/B edufit yes	Coefficient 4554119 0851138 3.144718 .7638799	Std. err. .3615579 .0822504 .6200539 .3613688	z -1.26 -1.03 5.07 2.11	<pre>P&gt; z  0.208 0.301 0.000 0.035</pre>	[95% conf. -1.164052 2463216 1.929434 .0556102	interval] .2532285 .0760939 4.360001 1.47215
pref female yes age grades A/B edufit yes	Coefficient 4554119 0851138 3.144718 .7638799	Std. err. .3615579 .0822504 .6200539 .3613688	z -1.26 -1.03 5.07 2.11	<pre>P&gt; z  0.208 0.301 0.000 0.035</pre>	[95% conf. -1.164052 2463216 1.929434 .0556102	interval] .2532285 .0760939 4.360001 1.47215
pref female yes age grades A/B edufit yes workexp internship	Coefficient 4554119 0851138 3.144718 .7638799 1.89448	Std. err. .3615579 .0822504 .6200539 .3613688	z -1.26 -1.03 5.07 2.11 3.01	<pre>P&gt; z  0.208 0.301 0.000 0.035 0.003</pre>	[95% conf. -1.164052 2463216 1.929434 .0556102 .6599679	interval] .2532285 .0760939 4.360001 1.47215 3.128992
pref female yes age grades A/B edufit yes workexp internship one year	Coefficient 4554119 0851138 3.144718 .7638799 1.89448 2.9124	Std. err. .3615579 .0822504 .6200539 .3613688 .6298646 .6203927	z -1.26 -1.03 5.07 2.11 3.01 4.69	<pre>P&gt; z  0.208 0.301 0.000 0.035 0.003 0.003</pre>	[95% conf. -1.164052 2463216 1.929434 .0556102 .6599679 1.696452	interval] .2532285 .0760939 4.360001 1.47215 3.128992 4.128347
pref female yes age grades A/B edufit yes workexp internship one year	Coefficient 4554119 0851138 3.144718 .7638799 1.89448 2.9124	Std. err. .3615579 .0822504 .6200539 .3613688 .6298646 .6203927	z -1.26 -1.03 5.07 2.11 3.01 4.69	<pre>P&gt; z  0.208 0.301 0.000 0.035 0.003 0.003</pre>	[95% conf. -1.164052 2463216 1.929434 .0556102 .6599679 1.696452	interval] .2532285 .0760939 4.360001 1.47215 3.128992 4.128347
pref female yes age grades A/B edufit yes workexp internship one year boardexp	Coefficient 4554119 0851138 3.144718 .7638799 1.89448 2.9124	Std. err. .3615579 .0822504 .6200539 .3613688 .6298646 .6203927	z -1.26 -1.03 5.07 2.11 3.01 4.69	<pre>P&gt; z  0.208 0.301 0.000 0.035 0.003 0.003</pre>	[95% conf. -1.164052 2463216 1.929434 .0556102 .6599679 1.696452	interval] .2532285 .0760939 4.360001 1.47215 3.128992 4.128347
pref female yes age grades A/B edufit yes workexp internship one year boardexp yes	Coefficient 4554119 0851138 3.144718 .7638799 1.89448 2.9124 .8102527	Std. err. .3615579 .0822504 .6200539 .3613688 .6298646 .6203927 .3972321	z -1.26 -1.03 5.07 2.11 3.01 4.69 2.04	<pre>P&gt; z  0.208 0.301 0.000 0.035 0.003 0.003 0.0041</pre>	[95% conf. -1.164052 2463216 1.929434 .0556102 .6599679 1.696452 .031692	interval] .2532285 .0760939 4.360001 1.47215 3.128992 4.128347 1.588813

Focusing only on the variables whose coefficients are significant at the 10% level (we are analyzing 8 respondents only!), we can write the estimated value of an applicant for a job of type 1 (research positions) as

value = 3.14\*(A/B grades) + 0.76\*edufit + 1.89\*internship + 2.91\*(1-year workexp) + 0.81\*boardexp

Thus, employers prefer applicants for a research position (job==1) whose educational portfolio fits the job, who have better grades, who have more relevant work experience, and who have (extracurricular) board experience. They do not seem to care much about the sex and age of applicants, which is comforting.

Given these estimates of the valuation by employers, we consider the probabilities that each of the applications is ranked first. Under the assumption that the  $\epsilon_i$  are independent and follow an extreme value type I distribution, Luce (1959) showed that the probability,  $\pi_i$ , that alternative *i* is valued higher than alternatives 2,..., *k* can be written in the multinomial logit form

$$\pi_i = \Pr \{ \text{value}_1 > \max(\text{value}_2, \dots, \text{value}_m) \} = \frac{\exp(\text{value}_i)}{\sum_{i=1}^k \exp(\text{value}_i)}$$

We fit our model:

The probability of observing a specific ranking can be written as the product of such terms, representing a sequential decision interpretation in which the rater first chooses the most preferred alternative, and then the most preferred alternative among the rest, etc.

The probabilities for alternatives to be ranked first are conveniently computed by predict.

```
. predict p if e(sample)
(option pr assumed; conditional probability that alternative is ranked first)
(210 missing values generated)
```

- . sort caseid pref p
- . list pref p grades edufit workexp boardexp if caseid==7, noobs

pref	р	grades	edufit	workexp	boardexp
0	.0021934	C/D	yes	none	yes
0	.0043086	C/D	no	internship	yes
0	.0051824	A/B	no	none	no
0	.0179498	C/D	yes	one year	no
1	.0403597	C/D	yes	one year	yes
2	.0226441	A/B	yes	none	no
3	.2642474	A/B	yes	one year	no
4	.0322894	A/B	yes	none	yes
5	.1505625	A/B	yes	internship	no
6	.4602626	A/B	yes	one year	yes

There clearly is a positive relation between the stated ranking and the predicted probabilities for alternatives to be ranked first, but the association is not perfect. In fact, we would not have expected a perfect association, because the model specifies a (nondegenerate) probability distribution over the possible rankings of the alternatives. These predictions for sets of 10 candidates can also be used to make predictions for subsets of the alternatives. For instance, suppose that only the last three candidates listed in this table would be available. According to parameter estimates of the rank-ordered logit model, the probability that the last of these candidates is selected equals 0.460/(0.032 + 0.151 + 0.460) = 0.715.

#### Comparing respondents

The cmrologit model assumes that all respondents, HR managers in large public-sector organizations in The Netherlands, use the same valuation function; that is, they apply the same decision weights. This is the substantive interpretation of the assumption that the  $\beta$ 's are constant between the respondents. To probe this assumption, we could test whether the coefficients vary between different groups of respondents. For a metric characteristic of the HR manager, such as firmsize, we can consider a trend model in the valuation weights,

$$\beta_{ij} = \alpha_{i0} + \alpha_{i1} \texttt{firmsize}_j$$

and we can test that the slopes  $\alpha_{i1}$  of firmsize are zero.

. generate fin	rmsize = emplo	yer				
<pre>. cmrologit pr &gt; c.firmsize#( &gt; if job==1, r</pre>	ref i.edufit i (1.edufit 1.gr nolog	.grades i.w ades 1.work	orkexp exp 2.woi	rkexp 1.b	ooardexp)	
Rank-ordered 1 Case ID variat	Number Number	of obs = of cases =	80 8			
Ties adjustmer	nt: No ties in	data		Obs per	case:	
				-	min = avg = max =	10 10.00 10
Log likelihood	1 = -66.49266			LR chi2 Prob >	2(9) = chi2 =	57.84 0.0000
pref	Coefficient	Std. err.	Z	P> z	[95% conf.	interval]
edufit yes	1.163862	1.134384	1.03	0.305	-1.059489	3.387213
grades A/B	6.657894	2.401567	2.77	0.006	1.950908	11.36488
workexp internship one year	2.346752 2.78297	1.908085 1.794268	1.23 1.55	0.219 0.121	-1.393026 7337314	6.08653 6.299672
edufit# c.firmsize yes	0118484	.0708709	-0.17	0.867	1507529	.127056
grades# c.firmsize A/B	217949	.1277188	-1.71	0.088	4682733	.0323753
workexp# c.firmsize internship one year	0353952 .0078179	.107952 .1125715	-0.33 0.07	0.743 0.945	2469773 2128183	.1761869 .228454
boardexp# c.firmsize yes	.0426636	.0235837	1.81	0.070	0035596	.0888868
. testparm c.f	firmsize#(i.ed	ufit i.grad	es i.worł	kexp i.bo	ardexp)	

```
(1) 1.edufit#c.firmsize = 0
```

```
( 2) 1.grades#c.firmsize = 0
( 3) 1.workexp#c.firmsize = 0
( 4) 2.workexp#c.firmsize = 0
( 5) 1.boardexp#c.firmsize = 0
```

chi2( 5) = 7.48

```
Prob > chi2 = 0.1871
```

The Wald test that the slopes of the interacted firmsize variables are jointly zero provides no evidence upon which we would reject the null hypothesis; that is, we do not find evidence against the assumption of constant valuation weights of the attributes by firms of different size. We did not enter firmsize as a predictor variable. Characteristics of the decision-making agent do not vary between alternatives. Thus, an additive effect of these characteristics on the valuation of alternatives does not affect the agent's ranking of alternatives and his or her choice. Consequently, the coefficient of firmsize is not identified. cmrologit would in fact have diagnosed the problem and dropped

firmsize from the analysis. Diagnosing this problem can slow the estimation considerably; the test may be suppressed by specifying the notestrhs option.

#### Incomplete rankings and ties

cmrologit allows incomplete rankings and ties in the rankings as proposed by Allison and Christakis (1994). cmrologit permits rankings to be incomplete only "at the bottom"; namely, that the ranking of the least attractive alternatives for subjects may not be known—do not confuse this with the situation that a subject is indifferent between these alternatives. This form of incompleteness occurred in the example discussed here because the respondents were instructed to select and rank only the top six alternatives. It may also be that respondents refused to rank the alternatives that are very unattractive.

cmrologit does not allow other forms of incompleteness, for instance, data in which respondents indicate which of four cars they like best, and which one they like least, but not how they rank the two intermediate cars. Another example of incompleteness that cannot be analyzed with cmrologit is data in which respondents select the three alternatives they like best but are not requested to express their preferences among the three selected alternatives.

cmrologit also permits ties in rankings. cmrologit assumes that if a subject expresses a tie between two or more alternatives, he or she actually holds one particular strict preference ordering, but with all possibilities of a strict ordering consistent with the expressed weak ordering being equally probable.

For instance, suppose that a respondent ranks alternative 1 highest. He or she prefers alternatives 2 and 3 over alternative 4 and is indifferent between alternatives 2 and 3. We assume that this respondent has the strict preference ordering either 1 > 2 > 3 > 4 or 1 > 3 > 2 > 4, with both possibilities being equally likely. From a psychometric perspective, it may actually be more appropriate to also assume that the alternatives 2 and 3 are close; for instance, the difference between the associated valuations (utilities) is less than some threshold or minimally discernible difference. Computationally, however, this is a more demanding model.

#### Clustered choice data

We have seen that applicants with work experience are in a relatively favorable position. To test whether the effects of work experience vary between the jobs, we can include interactions between the type of job and the attributes of applicants. Such interactions can be obtained using factor variables.

Because some HR managers contributed data for more than one job, we cannot assume that their selection decisions for different jobs are independent. We can account for this by specifying the vce(cluster clustvar) option. By treating choice data as incomplete ranking data with only the most preferred alternative marked, cmrologit may be used to estimate the model parameters for clustered choice data.

. cmrologit pref job##(i.female i.grades i.edufit i.workexp), > vce(cluster employer) nolog note: 2.job 3.job omitted because of no within-case variance. Rank-ordered logit choice model Number of obs 290 = Case ID variable: caseid Number of cases 29 = Ties adjustment: efron Obs per case: min = 10 avg = 10.00 max = 10 Wald chi2(15) = 93.03 Log pseudolikelihood = -296.08 Prob > chi2 = 0.0000 (Std. err. adjusted for 22 clusters in employer)

Robust Coefficient std. err. P>|z| [95% conf. interval] pref z job managemen.. 0 (omitted) policy ad.. 0 (omitted) female -.2249088 .2396552 -0.94 0.348 -.6946244 .2448068 yes grades 2.847569 0.000 1.262475 A/B .8087366 3.52 4.432664 edufit .6759788 .2318277 2.92 0.004 .2216049 1.130353 yes workexp internship 1.450487 .5518405 2.63 0.009 .3689 2.532075 one year 2.495849 .72438 3.45 0.001 1.07609 3.915608 job#female managemen.. # .0227426 .4749959 -.9082322 0.05 0.962 .9537174 yes policy ad.. # .1138279 .3559085 0.32 0.749 -.58374.8113958 yes job#grades managemen.. # A/B -2.381741.9589772 -2.480.013 -4.261302-.50218 policy ad.. # A/B -1.92171.8563522 -2.240.025 -3.60013 -.2432907job#edufit managemen.. # .4041935 -.2427363-0.60 0.548 -1.034941.5494684 yes policy ad.. # -.2942018.3578419 -0.82 0.411 -.9955589 .4071553 yes job#workexp managemen.. # internship -1.183344.7275346 -1.63 0.104 -2.609286.2425972 managemen.. # one year -1.495627.7763694 -1.930.054 -3.017283.0260292 policy ad.. # internship -.6353285 .8809524 -0.72 0.471 -2.361963 1.091306 policy ad.. # one year -.95225991.02415 -0.93 0.352 -2.9595561.055036 The parameter estimates for the first job type are very similar to those that would have been obtained from an analysis isolated to these data. Differences are due only to an implied change in the method of handling ties. With clustered observations, cmrologit uses Efron's method. If we had specified the ties(efron) option with the separate analyses, then the parameter estimates would have been identical to the simultaneous results.

Another difference is that cmrologit now reports robust standard errors, adjusted for clustering within respondents. These could have been obtained for the separate analyses, as well by specifying the vce(robust) option. In fact, this option would also have forced cmrologit to switch to Efron's method as well.

Given the combined results for the three types of jobs, we can test easily whether the weights for the attributes of applicants vary between the jobs, in other words, whether employers are looking for different qualifications in applicants for different jobs. A Wald test for the equality hypothesis of no difference can be obtained with the testparm command:

```
. testparm job#(i.female i.grades i.edufit i.workexp)
 (1)
      2.job#1.female = 0
 (2)
      3.job#1.female = 0
 ( 3) 2.job#1.grades = 0
 ( 4) 3.job#1.grades = 0
 ( 5) 2.job#1.edufit = 0
 ( 6) 3.job#1.edufit = 0
 (7) 2.job#1.workexp = 0
 (8) 2.job#2.workexp = 0
 ( 9) 3.job#1.workexp = 0
 (10) 3.job#2.workexp = 0
          chi2(10) =
                        18.01
        Prob > chi2 =
                         0.0548
```

We find only mild evidence that employers look for different qualities in candidates according to the job for which they are being considered.

#### Technical note

Allison (1999) stressed that the comparison between groups of the coefficients of logistic regression is problematic, especially in its latent-variable interpretation. In many common latent-variable models, only the regression coefficients divided by the scale of the latent variable are identified. Thus, a comparison of logit regression coefficients between, say, men and women is meaningful only if one is willing to argue that the standard deviation of the latent residual does not differ between the sexes.

The rank-ordered logit model is also affected by this problem. While we formulated the model with a scale-free residual, we can actually think of the model for the value of an alternative as being scaled by the standard deviation of the random term, representing other relevant attributes of alternatives. Again, comparing attribute weights between jobs is meaningful to the extent that we are willing to defend the proposition that "all omitted attributes" are equally important for different kinds of jobs.

#### Comparison of cmrologit and clogit

The rank-ordered logit model also has a sequential interpretation. A subject first chooses the best among the alternatives. Next, he or she selects the best alternative among the remaining alternatives, etc. The decisions at each of the subsequent stages are described by a conditional logit model, and a subject is assumed to apply the same decision weights at each stage. Some authors have expressed concern that later choices may well be made more randomly than the first few decisions. A formalization of this idea is a heteroskedastic version of the rank-ordered logit model in which the scale of the random term increases with the number of decisions made (for example, Hausman and Ruud [1987]). This extended model is currently not supported by cmrologit. However, the hypothesis that the same decision weights are applied at the first stage and at later stages can be tested by applying a Hausman test.

First, we fit the rank-ordered logit model on the full ranking data for the first type of job.

. cmrologit pr	ref age i.fema	le i.edufit	i.grades	i.boarde:	xp if j	job==1,	nolog
Rank-ordered 1	logit choice m	odel		Number of	f obs	=	80
Case ID variab	Case ID variable: caseid					3 =	8
Ties adjustmer	nt: No ties in	data		Obs per o	case:		
					r	nin =	10
					a	avg =	10.00
					n	nax =	10
				LR chi2(	5)	=	26.15
Log likelihood	1 = -82.33537			Prob > cl	hi2	=	0.0001
pref	Coefficient	Std. err.	z	P> z	[95%	conf.	interval]
age	1160121	.0767137	-1.51	0.130	2663	3682	.0343439
female yes	0791295	.3354377	-0.24	0.814	7365	5753	.5783163
edufit yes	.2475177	.3186609	0.78	0.437	3770	0462	.8720817
grades A/B	1.866381	.4542095	4.11	0.000	.9761	1463	2.756615
boardexp yes	0418455	.3194106	-0.13	0.896	6678	3788	.5841878

Second, we save the estimates for later use with the estimates command.

. estimates store Ranking

Third, to estimate the decision weights on the basis of the most preferred alternatives only, we create a variable, best, that is 1 for the best alternatives and 0 otherwise. The by prefix is useful here.

. by caseid (pref), sort: generate best = (pref == pref[\_N]) if job==1 (210 missing values generated)

By specifying (pref) with by caseid, we ensured that the data were sorted in increasing order on pref within caseid. Hence, the most preferred alternatives are last in the sort order. The expression pref == pref [\_N] is true (1) for the most preferred alternatives, even if the alternative is not unique, and false (0) otherwise.

If the most preferred alternatives were sometimes tied, we could still fit the model for the basedalternatives-only data via cmrologit, but clogit would yield different results because it deals with ties in a less appropriate way for continuous valuations. To ascertain whether there are ties in the selected data regarding applicants for research positions, we can combine by with assert:

. by caseid (pref), sort: assert pref[\_N-1] != pref[\_N] if job==1

There are no ties. We can now fit the model on the choice data by using either clogit or cmrologit.

. cmrologit be	est age i.eduf	it i.grades	i.boarde	exp if jo	b==1, nolog	
Rank-ordered logit choice model Case ID variable: caseid					of obs = of cases =	80 8
Ties adjustmer	nt: No ties in	data		Obs per	case:	
5				Ĩ	min = avg = max =	10 10.00 10
Log likelihood	d = −16.25952			LR chi2 Prob >	2(4) = chi2 =	4.32 0.3641
best	Coefficient	Std. err.	z	P> z	[95% conf	. interval]
age	0552291	.1887951	-0.29	0.770	4252607	.3148024
edufit yes	049965	.7530442	-0.07	0.947	-1.525905	1.425975
grades A/B	1.505808	1.11493	1.35	0.177	6794136	3.69103
boardexp yes	.995195	.8461853	1.18	0.240	6632977	2.653688

. estimates store Choice

The same results, though with a slightly different formatted header, would have been obtained by using clogit on these data.

. clogit best	age i.edufit	i.grades i.	boardexp	if job=	<pre>=1, group(case;</pre>	id) nolog
Conditional (1	fixed-effects)	logistic r	regression	ı	Number of ob: LR chi2(4)	s = 80 = 4.32
Log likelihood	d = −16.259518	1			Prob > chi2 Pseudo R2	= 0.3641 = 0.1173
best	Coefficient	Std. err.	Z	P> z	[95% conf.	interval]
age	0552291	.1887951	-0.29	0.770	4252607	.3148024
edufit yes	049965	.7530442	-0.07	0.947	-1.525905	1.425975
grades A/B	1.505808	1.11493	1.35	0.177	6794136	3.69103
boardexp yes	.995195	.8461853	1.18	0.240	6632977	2.653688

The parameters of the ranking and choice models look different, but the standard errors based on the choice data are much larger. Are we estimating parameters with the ranking data that are different from those with the choice data? A Hausman test compares two estimators of a parameter. One of the estimators should be efficient under the null hypothesis, namely, that choosing the second-best alternative is determined with the same decision weights as the best, etc. In our case, the efficient estimator of the decision weights uses the ranking information. The other estimator should be consistent, even if the null hypothesis is false. In our application, this is the estimator that uses the first-choice data only.

. hausman Choi	. hausman Choice Ranking						
Coefficients							
	(b)	(B)	(b-B)	<pre>sqrt(diag(V_b-V_B))</pre>			
	Choice	Ranking	Difference	Std. err.			
age	0552291	1160121	.060783	.1725068			
1.edufit	049965	.2475177	2974828	.6822982			
1.grades	1.505808	1.866381	3605724	1.018215			
1.boardexp	.995195	0418455	1.037041	.7835857			
	b = Co	nsistent under	HO and Ha; obta	ained from cmrologit.			
B = Inc	consistent unde	r Ha, efficien	nt under HO; obta	ained from <b>cmrologit</b> .			
Test of HO: Di	fference in co	efficients not	systematic				
chi2(4) =	(b-B),[(V_b-V_	B)^(-1)](b-B)					
= Prob > chi2 =	0.6672						

We do not find evidence for misspecification. We have to be cautious, though, because Hausmantype tests are often not powerful, and the number of observations in our example is very small, which makes the quality of the method of the null distribution by a  $\chi^2$  test rather uncertain.

#### On reversals of rankings

The rank-ordered logit model has a property that you may find unexpected and even unfortunate. Compare two analyses with the rank-ordered logit model, one in which alternatives are ranked from "most attractive" to "least attractive", the other a reversed analysis in which these alternatives are ranked from "most unattractive" to "least unattractive". By unattractiveness, you probably mean just the opposite of attractiveness, and you expect that the weights of the attributes in predicting "attractiveness" to be minus the weights in predicting "unattractiveness". This is, however, *not* true for the rank-ordered logit model.

The assumed distribution of the random residual takes the form  $F(\epsilon) = 1 - \exp\{\exp(-\epsilon)\}$ . This distribution is right skewed. Therefore, slightly different models result from adding and subtracting the random residual, corresponding with high-to-low and low-to-high rankings. Thus, the estimated coefficients will differ between the two specifications, though usually not in an important way.

You may observe the difference by specifying the reverse option of cmrologit. Reversing the rank order makes rankings that are incomplete at the bottom become incomplete at the top. Only the first kind of incompleteness is supported by cmrologit. Thus, for this comparison, we exclude the alternatives that are not ranked, omitting the information that ranked alternatives are preferred over excluded ones.

- . cmrologit pref grades edufit workexp boardexp if job==1 & pref!=0
   (output omitted)
- . estimates store Original
- . cmrologit pref grades edufit workexp boardexp if job==1 & pref!=0, reverse
   (output omitted)
- . estimates store Reversed

Variable	Original	Reversed
grades A/B	1.9842801	-1.2118836
edufit yes	16397461	11698355
workexp internship one year	.50190232 2.3208572	70220848 -2.1518673
boardexp yes	.32930412	19747927
aic bic	97.817471 107.17348	101.24092 110.59692

. estimates table Original Reversed, stats(aic bic)

Thus, although the weights of the attributes for reversed rankings are indeed mostly of opposite signs, the magnitudes of the weights and their standard errors differ. Which one is more appropriate? We have no advice to offer here. The specific science of the problem will determine what is appropriate, though we would be surprised indeed if this helps here. Formal testing does not help much either because the models for the original and reversed rankings are not nested. The model-selection indices, such as the AIC and BIC, however, suggest that you stick to the rank-ordered logit model applied to the original ranking rather than to the reversed ranking.

## Stored results

cmrologit stores the following in e():

Scalars			
e(N)	number of observations		
e(N_case)	number of cases		
e(N_ic)	N for Bayesian information criterion (BIC)		
e(N_clust)	number of clusters		
e(df_m)	model degrees of freedom		
e(11)	log likelihood		
e(11_0)	log likelihood of the null model ("all rankings are equiprobable")		
e(chi2)	$\chi^2$		
e(r2_p)	pseudo- $R^2$		
e(p)	<i>p</i> -value for model test		
e(code_inc)	value for incomplete preferences		
e(alt_min)	minimum number of alternatives		
e(alt_avg)	average number of alternatives		
e(alt_max)	maximum number of alternatives		
e(rank)	rank of e(V)		
e(converged)	1 if converged, 0 otherwise		
Macros			
e(cmd)	cmrologit		
e(cmdline)	command as typed		
e(depvar)	name of dependent variable		
e(caseid)	name of case ID variable		
e(wtype)	weight type		
e(wexp)	weight expression		
e(marktype)	casewise or altwise, type of markout		
e(key_N_ic)	cases, key for $N$ for Bayesian information criterion (BIC)		

	e(title)	title in estimation output
	e(clustvar)	name of cluster variable
	e(offset)	linear offset variable
	e(chi2type)	Wald or LR; type of model $\chi^2$ test
	e(reverse)	reverse, if specified
	e(ties)	breslow, efron, exactm
	e(vce)	vcetype specified in vce()
	e(vcetype)	title used to label Std. err.
	e(properties)	b V
	e(predict)	program used to implement predict
	e(marginsok)	predictions allowed by margins
	e(marginsnotok)	predictions disallowed by margins
	e(marginsdefault)	default predict() specification for margins
	e(asbalanced)	factor variables fvset as asbalanced
	e(asobserved)	factor variables fvset as asobserved
Mat	rices	
	e(b)	coefficient vector
	e(V)	variance-covariance matrix of the estimators
	e(V_modelbased)	model-based variance
Fund	ctions	
	e(sample)	marks estimation sample
	•	*

In addition to the above, the following is stored in r():

Matrices r(table)

matrix containing the coefficients with their standard errors, test statistics, *p*-values, and confidence intervals

Note that results stored in r() are updated when the command is replayed and will be replaced when any r-class command is run after the estimation command.

## Methods and formulas

Allison and Christakis (1994) demonstrate that maximum likelihood estimates for the rank-ordered logit model can be obtained as the maximum partial-likelihood estimates of an appropriately specified Cox regression model for waiting time ([ST] stcox). In this analogy, a higher ranking of an alternative is formally equivalent to a higher hazard rate of failure. cmrologit uses stcox to fit the rank-ordered logit model based on such a specification of the data in Cox terms. A higher stated preference is represented by a shorter waiting time until failure. Incomplete rankings are dealt with via censoring. Moreover, decision situations (subjects) are to be treated as strata.

Finally, as proposed by Allison and Christakis, ties in rankings are handled by the marginallikelihood method, specifying that all strict preference orderings consistent with the stated weak preference ordering are equally likely. The marginal-likelihood estimator is available in stcox via the exactm option. The methods of the marginal likelihood due to Breslow and Efron are also appropriate for the analysis of rank-ordered logit models. Because in most applications the number of ranked alternatives by one subject will be fairly small (at most, say, 20), the number of ties is small as well, and so you rarely will need to turn to methods to restrict computer time. Because the marginal-likelihood estimator in stcox does not support the cluster adjustment or pweights, you should use the Efron method in such cases.

This command supports the clustered version of the Huber/White/sandwich estimator of the variance using vce(robust) and vce(cluster *clustvar*). See [P] <u>robust</u>, particularly *Maximum likelihood estimators* and *Methods and formulas*. Specifying vce(robust) is equivalent to specifying vce(cluster *caseid*), where *caseid* is the variable that identifies the cases.

### Acknowledgment

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### Also see

- [CM] **cmrologit postestimation** Postestimation tools for cmrologit
- [CM] cmclogit Conditional logit (McFadden's) choice model
- [CM] **cmroprobit** Rank-ordered probit choice model
- [CM] **cmset** Declare data to be choice model data
- [R] ologit Ordered logistic regression
- [U] 20 Estimation and postestimation commands

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